

# Various Forms of Bias Analysis for

Various Forms of Bias Analysis for  
Observational Research  
Uncontrolled Confounding in

Department of Epidemiology, UCLA Fielding School of Public Health  
Department of Statistics, UCLA, Los Angeles, California

# Uncontrolled Confounding in Observational Research

Department of Epidemiology, UCLA Fielding School of Public Health Department  
of Statistics, UCLA, Los Angeles, California

# Outline

- Background
- State of the Art

- Future Directions
- Conclusion

- Key sources of bias or systematic error:
  - Confounding
  - Selection bias

- Measurement error (misclassification)
- These sources of bias are often neglected in large studies or meta-analyses where they matter most
- Recent advancements in methods and computing have made it easier to conduct bias analysis

**Data we want but do not have id U X Y**

1

2

3

:

.

:

.

N

**Data we have**

id  $U(X) X^* Y$

1

2

3

:

.

:

.

N



## Missing data



- Bias sources can occur singly, jointly or be repeated over time
- Models for the bias must address the above single or multiple bias scenarios and their appropriate sequence
- Bias sources can be seen as inducing missing data and can be

depicted in directed acyclic graphs (DAGS)

**C U**









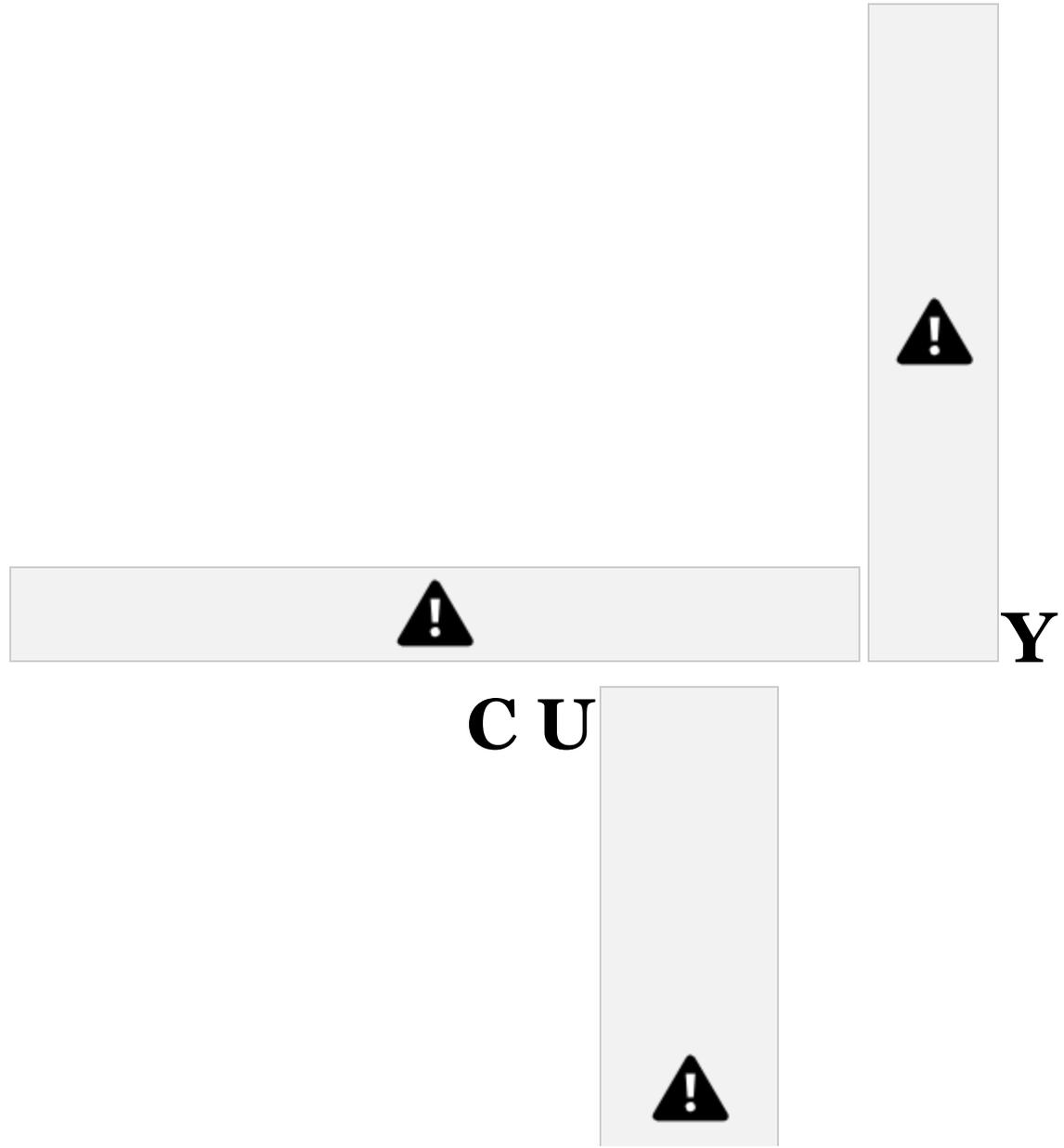


**C U**





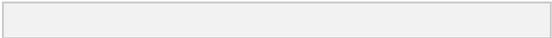
**X**







**Y**



- Not adjusting for  $U$  leads to
  - **Uncontrolled confounding** of conditional and marginal effects of  $X$  on  $Y$
  - **Collider-stratification bias** in the association of  $C$  and  $Y$  (hence, the so-called **table 2 fallacy**)
  - **Amplification of bias** in  $X \square Y$  association if we additionally adjust for an instrumental variable (i.e. a variable associated only with  $X$  but not  $U$  or  $C$ , and with  $Y$  only through  $X$ )



# State of the Art



- Current methods for bias analysis of uncontrolled confounding (typically based on the back door

criterion) fall into one of these broad categories:

- **Bias formula methods**
- **Missing data methods**
- **Negative control methods**
- **Bounding methods**



# Bias Formulas

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Epidemiological Association ! The Author 2009; all rights reserved. Advance  
Access publication 22 September 2009

International Journal of Epidemiology 2009;38 :1175–1191  
doi:10.1093/ije/dyp289

## REPRINTS AND REFLECTIONS

# Smoking and lung cancer: recent evidence and a discussion of some questions<sup>1</sup>

Jerome Cornfield,<sup>1</sup> William Haenszel,<sup>2</sup> E. Cuyler Hammond,<sup>3</sup> Abraham M. Lilienfeld,<sup>4</sup> Michael B.  
Shimkin<sup>5</sup> and Ernst L. Wynder<sup>6</sup>

**Summary** This report reviews some of the more recent epidemiologic and experimental findings on the relationship of tobacco smoking to lung cancer, and discusses some criticisms directed against the conclusion that tobacco smoking, especially cigarettes, has a causal role in the increase in broncho-genic carcinoma. The magnitude of the excess lung-cancer risk among cigarette smokers is so great that the results can not be interpreted as arising from an indirect association of cigarette smoking with some other agent or characteristic, since this hypothetical agent would have to be at least as strongly

associated with lung cancer as cigarette use; no such agent has been found or suggested. The consistency of all the epidemiologic and experimental evidence also supports the conclusion of a causal relationship with cigarette smoking, while there are serious inconsistencies in reconciling the evidence with other hypotheses which have been advanced. Unquestionably there are areas where more research is necessary, and, of course, no single cause accounts for all lung cancer. The information already available, however, is sufficient for planning and activating public health programs.

– J. Nat. Cancer Inst. 22:173–203, 1959.



In 1957 a Study Group<sup>1</sup>, appointed by the National Commission on Cancer, concurrently, a report from the Medical Research Service, U.S. Department of Health, Education and Welfare, on the use of conditional estimate.

## Bias Formulas for External Adjustment and Sensitivity Analysis

RESULTS: All the bias expressions can be given parallel formulations as the difference or ratio of (i) the sum across confounder strata of each exposure-stratified confounder-outcome effect measure multiplied by the confounder prevalences among the exposed and (ii) the sum across confounder strata of the same effect measure multiplied by the confounder prevalences among the unexposed. The basic formulas can be applied to scenarios with a polytomous confounder, exposure, or outcome.

CONCLUSIONS: In addition to aiding design and analysis strategies for confounder control, the bias formulas provide a link between classical standardization decompositions of demography and classical bias formulas of epidemiology. They are also useful in constructing general programs for sensitivity analysis and more elaborate probabilistic risk analyses.

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ONLINE EDITION  
DOI: 10.1111/j.1749-7628.2010.02411.x  
Ann Epidemiol 2008;18:637–646. © 2008 Elsevier Inc. All rights reserved.

KEY WORDS: Bias, Bias Adjustment, Confounding, Epidemiologic Methods, Odds Ratio, Risk Difference,  
Submitted 4 March 2010; accepted 10 August 2010.

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Supported by National Institutes of Health grant R03 HD060696 – 0 (to T.J.V.). Supported by a career grant (VENI number 916.96).

ORIGINAL ARTICLE

from the Netherlands Organization for Scientific Research (NWO/A.A.).



Supplemental digital content is available through direct URL citatin the HTML and PDF versions of this article (www.epidem.coCorrespondence: Tyler J. VanderWeele, Departments of Epidemiology

# Bias Formulas for Sensitivity Analysis of Unmeasured

PURPOSE: Uncontrolled confounders are an important source of bias in epidemiologic studies. risk ratio, and

The au Risk Ratio, Sensitivity Analysis, Unmeasured Confounders.

Biostatistics, Harvard School of Public Health, 677 Huntington Ave

thors review and derive a set of parallel simple formulas for bias factors in the risk difference,

## Confounding for General Outcomes, Treatments,

## and Confounders

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DOI: 10.1097/EDE.0b013e3181f74493

Tyler J. VanderWeele<sup>a,b</sup> and Onyebuchi A. Arah<sup>c,d</sup>

studies with an unmeasured polytomous confounder and a dichotomous exposure and outcome.

METHODS: The authors show how the bias formulas are related to and are sometimes simpler than earlier (RR) in from cohort studies and the odds ratio (OR) in case-con

formulas. The article contains three examples, including a Monte Carlo sensitivity analysis of a preadjusted Boston, MA 02115. E-mail: tvanderw@hsph.harvard.edu.

e central problems in causal inference from obser trol studies can be given a common conceptual framework. We show how the basic formulas can be straightforwardly

or conditional estimate.

RESULTS: All the bias expressions can be given parallel formulations as the difference or ratio of (i) the

*Epidemiology* • Volume 22, Number 1, January 2011

ata is uncontrolled confounding (1). This problem ~~expe~~

applied to scenarios with a polytomous ~~us confounder,~~

sum across confounder strata of each exposure-stratified confounder-outcome effect ~~ense~~ sensitive review, a number of the existing techniques are measure multiplied by

s from insufficient knowledge of important con

restricted to simple or very particular settings. There is

**Abstract:** Uncontrolled confounding in observational studies

the confounder prevalences among the exposed and (ii) the sum across confounder are re

strata of the same effect sure, or outcome. We also describe how the formulas gives rise to biased effect estimates. Sensitivity analysis tech measure multiplied by the confounder prevalences among the unexposed. The basic

UCTION



formulas can be applied

also a literature on bounds for causal effects or “partial

or lack of data on known potential confounders.

niques can be useful in assessing the magnitude of these biases.

to scenarios with a polytomous confounder, exposure, or outcome.

earchers discuss potential bias from failing to ad

Monte Carlo sensitivity analysis. We will discuss cohort

CONCLUSIONS: In addition to aiding design and analysis strategies for confounder control, the bias for

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analysis and

additive, risk-ratio and odds-ratio scales. We show that these

more elaborate probabilistic risk analyses.

by interpreting the denominators as person time, provided

ias formulas (1, Chapter [Ch.] 19). These formulas

to Cornfield et al. (2) and Bross (3, 4), have been

Ann Epidemiol 2008;18:637–646. ! 2008 Elsevier Inc. All rights

reserved.

methods in the statistics and epidemiology literature. The

the impact of exposure on the person-time is negligible (1

applicability, usefulness, and limits of the bias-adjustment for

Using the potential outcomes framework, we derive a

extensively since (5–15) and are often

used as

[Ch. 3], 4, 19).

doi: 10.1111/ppe.12049

mulas are discussed. We illustrate the sensitivity-analysis tech

general class of formulas for sensitivity analysis of uncon

KEY WORDS: Bias, Bias Adjustment, Confounding, Epidemiologic Methods, Odds Ratio, Risk Difference,

dern bias-analysis techniques (1, Ch. 19;

16–18).

show that the equations for biases from uncon

Commentary

formulas are particularly simple and

trolled confounding with outcomes, treatments, and mea sured and unmeasured

confounders that may be categorical

Risk Ratio, Sensitivity Analysis, Unmeasured Confounders.

niques that follow from our results by applying them to 3 different studies. The bias

## Marginal Structural Models, Doubly Robust Estimation, and

confounding in the risk difference (RD) and

risk ratio

### METHODS AND RESULTS

easy to use in settings in which the unmeasured confounding variable many previous results in the literature and give rise

is binary with constant effect on the outcome across

(2 or more categories) or continuous. The formulas generalize

treatment levels.

BMJ 2013;347:f4533 doi: 10.1136/bmj.f4533 (Published 30 July 2013) Page 1 of 11

# Bias Analysis in Perinatal and Paediatric Epidemiology to very flexible sensitivity-analysis techniques that can be

## INTRODUCTION Research

### Notation

(RR) in cohort studies and the odds ratio (OR) in case-control studies can be given a common conceptual framework.

used in a wide range of applications. We also describe a particularly easy-to-use sensitivity-analysis technique that

(*Epidemiology* 2011;22: 000 – 000)

Onyebuchi A. Arah,<sup>a,b</sup> Madhuri Sudan,<sup>a</sup> Jørn Olsen<sup>a,c</sup> and Leeka Kheifets<sup>a</sup>

We show how the basic formulas can be

straightforwardly can be used under some simplifying assumptions and that

Let  $A_{xz}$  represent cases,  $B_{xz}$  controls or noncases where  $D$

One of the central problems in causal inference from obser

f Amsterdam, The Netherlands (O.A.A.); Department of Ep

<sup>a</sup>Department of Epidemiology, The Fielding School of Public Health, University of California, Los Angeles, CA, USA

represents disease or outcome,  $X$  the exposure, and  $Z$  the un

observational data is uncontrolled confounding (1). This problem

follows from our results and is summarized in the discus

University of California, Los Angeles School of Public Health,

applied to scenarios with a polytomous confounder, expo (O.A.A., Y.C., S.G.); Department of Biostatistics, Kyoto Uni

measured confounder. Also, we use  $N_{xz}$  to represent the sum

sion section.

often stems from insufficient knowledge of important con ol of Public Health, Japan (Y.C.); and Department of Statistics,

<sup>c</sup>Institute of Public Health, University of Aarhus, Aarhus, Denmark in biased effect estimates. Several sensitivity-analysis

sure, or outcome. We also describe how the formulas are re

of  $A_{xz}$  and  $B_{xz}$ , that is, the total number exposed to  $X$   $Z$   $x$

founders or lack of data on known potential confounders.  $\dagger$  related to previously published work and illustrate their use

California, Los Angeles College of Letters and Science (S.G.).

in We thank Ahrens and Schisterman (henceforth, A&S)

door or when the exposure under study is cause

## NOTATION, DEFINITIONS, AND

and bias-modeling techniques have now been developed to correspondence to: Onyebuchi A. Arah, MD, PhD, Department

handle uncontrolled confounding.<sup>1-22</sup> Although the litera

within the stratum  $Z$   $Z$   $z$ . The prevalence of each stratum

When researchers discuss potential bias from failing to ad medicine, Academic Medical Center, University of Amsterdam,

Monte Carlo sensitivity analysis. We will discuss cohort for

## ASSUMPTIONS

for their commentary<sup>1</sup> on our article.<sup>2</sup> Although it was

ture is large and it would be difficult to provide a compre

collider that also lies on an open back-door path

of  $Z$  given exposure  $X$  is notated as  $P_{zx}$ . For any measure re

just for a confounder, they usually do so only qualitatively.

mulas in terms of risk differences and risk ratios,

although

## RESEARCH

Unmeasured confounders in observational studies result

<sup>b</sup>Department of Public Health, Academic Medical Center, University of Amsterdam, Amsterdam, The Netherlands

We will use the potential outcomes or counterfactual framework.<sup>28–30</sup> Let treatment  $A$  denote the treatment where the first subscript represents the ‘outcome’ (in this received by a particular individual. Let  $Y$  be the observed

## A more convincing approach uses external data in

ratios

adjust 31 20 697 2316. E-mail: [o.a.arah@amc.uva.nl](mailto:o.a.arah@amc.uva.nl),  
[arah@ucla.edu](mailto:arah@ucla.edu).

the same formulas apply to rate differences and rate invited discussion on the place of causal inference in

# Severe hypoglycaemia and cardiovascular disease:

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September 14, 2007; accepted April 2, 2008.

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by interpreting the denominators as person time, provided

received by a particular individual. Let  $Y$  be the observed

Submitted 4 March 2010; accepted 10 August 2010.

ture as probabilistic bias analysis is increa

From the Departments of <sup>a</sup>Epidemiology and <sup>b</sup>Biostatistics, Harvard School

perinatal and paediatric epidemiology. In response,

post-treatment outcome of that individual. Let  $Y_a$  denote

## systematic review and meta-analysis with bias analysis

date back to Cornfield et al. (2) and Bross (3, 4), have been

we briefly offer some clarifications and extensions. of Public Health, Boston, MA; <sup>c</sup>Department of Epidemiology, School of

accepted by journals, large data become more

the impact of exposure on the person-time is negligible (1

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Public Health, University of California, Los Angeles (UCLA), Los

developed extensively since (5–15) and [Ch. 3], 4, 19). are often used as

the potential outcome  $Y$  for an individual if the treatment

A&S claim that we did not adjust for reduced able, and investigators routinely use bias form

Angeles, CA; and <sup>d</sup>Department of Public Health, Academic Medical

venue South, New York, NY 10010 doi:10.1016/j.annepidem.2008.04.003

$A$ , perhaps contrary to fact, had been set to value  $a$ . Note

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hearing at age 18 months ( $Y_1$ ) in our analysis of the and simulation techniques. We disagree with

Health grant R03 HD060696 – 01A1

that we assume that the potential outcome  $Y_a$  for an

Herein we show that the equations for biases from

uncon

impact of postnatal cellphone exposure ( $X_2$ ) on

that bias analysis must be preceded by ‘placement’ individual does not depend on the treatments received by

(to T.J.V.). Supported by a career grant (VENI number 916.96.059)

hearing loss at age 7 years ( $Y_2$ ). In fact, we adjusted for

the unmeasured confounder in the DAG<sup>1</sup> an

from the Netherlands Organization for Scientific Research (NWO) (to

Atsushi Goto *senior researcher*<sup>1,2</sup>, Onyebuchi A Arah *professor*<sup>3,4</sup>, Maki Goto *researcher*<sup>1,2</sup>, Yasuo

other individuals. This assumption is sometimes referred

trolled confounding in the risk difference (RD) and risk ratio

to as SUTVA, the stable unit treatment value assumption<sup>30</sup>

METHODS AND RESULTS

$Y_i$  and other variables listed in the footnotes of Tables



such placement can reveal when 'the potential

Terauchi *professor*<sup>2</sup>, Mitsuhiro Noda *director*<sup>1</sup>

Supplemental digital content is available through direct URL citations

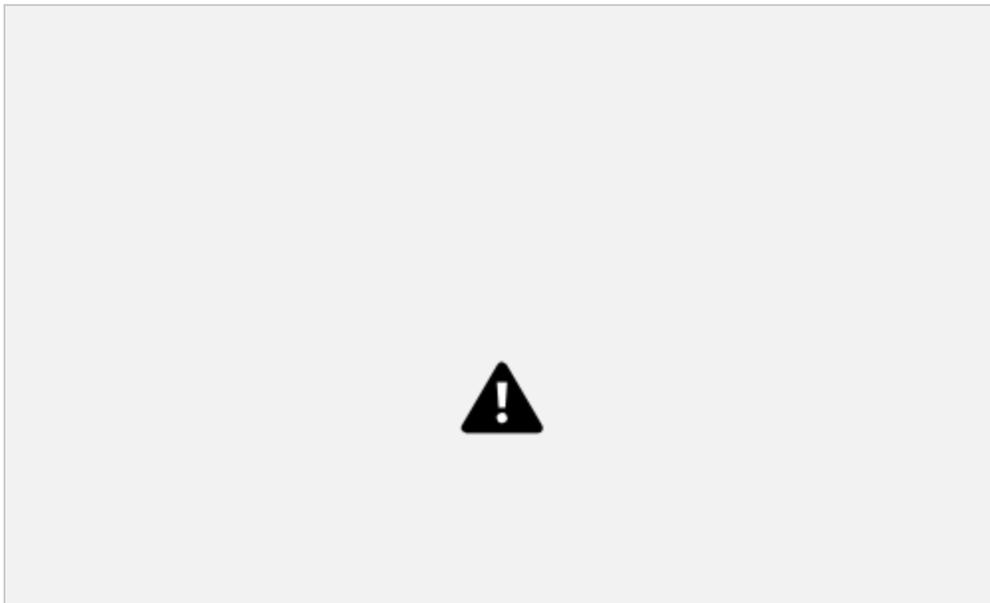
or as a no-interference assumption.<sup>31</sup> Furthermore, we

3 and 4 in our article.<sup>2</sup>In applying directed acyclic in the HTML and PDF versions of this article ([www.epidem.com](http://www.epidem.com)).

no longer a concern'.<sup>1</sup> A known but unmeasure

**Bias formula methods** trace and quantify the open back door path due to unmeasured  $U$ :  $X \square U \square Y$  conditional on  $C$

[C]



U



**[X]**





- At the core of bias analysis are the following expressions with the unknown part in gray, parts from observed data

highlighted in yellow, and what we want is in **bold blue**:

$$P(Y, U, X, C)$$

$$= P(Y | X, C, U) P(U | X, C) P(X, C) \quad \square \text{ Bias formula methods} =$$

$$P(U | Y, X, C) P(Y | X, C) P(X, C) \quad \square \text{ Missing data methods}$$



- External adjustment of crude or pre-adjusted association measures can be done using bias formulas for the bias model:

$$RD_{+} - RD_{adj} = Bias_{RD}$$

$$RR_{+} / RR_{adj} = Bias_{RR}$$

$$OR_{+} / OR_{adj} = Bias_{OR}$$

where  $RD_+$ ,  $RR_+$  and  $OR_+$  are respectively the crude or biased risk difference, risk ratio and odds ratio respectively;  $RD_{adj}$ ,  $RR_{adj}$  and  $OR_{adj}$  are their unknown “true” or confounding adjusted versions;

$Bias_{RD}$ ,  $Bias_{RR}$ , and  $Bias_{OR}$  are the respective *bias formulas* containing the **bias parameters** as shown on the following slides



- For conditional risk differences (i.e. conditioned on measured confounder  $C$ ), we have the following respective bias formulas:





- For marginal risk differences, we have the following respective bias formulas:





- Bias formulas can also be applied to record-level data by using a **bias offset** method
- Bias offset method computes an offset variable from the appropriate form of the bias formula and for the appropriate link function
  - Identity bias offset for risk difference and mean difference models:

- Compute  $BiasOffset = RD_{X \square U} \times RD_{U \square Y} \times X$
- Regress  $Y$  on  $X$  and  $C$  with  $BiasOffset$  set as an offset variable – Log

bias offset for risk ratio and odds ratio models



## Missing Data Methods

- Uncontrolled confounding is a special case of missing data: missing data on  $U$  for all study subjects
- While **bias formula methods** aim to compute the amount of bias

using exposure- $U$  and  $U$ -outcome relations, **missing data methods** aim to impute or simulate the missing (unmeasured) confounding variable  $U$

- Missing data methods are usually internal adjustment methods that simulate the missing data on  $U$  using validation study data or externally obtained information combined with the observed data on exposure, outcome and measured confounders or using propensity or disease risk scores

For example:  $P(Y, U, X, C) = P(U | Y, X, C)P(Y, X, C)$



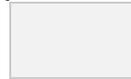
# Bayesian perspectives for epidemiologic research: III. Bias analysis via missing-data methods

Sander Greenland

Accepted 30 June 2009

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**American Journal of Epidemiology Advance Access  
published March 28, 2007**



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Public Health

DOI: 10.1093/aje/kwm074

I present some extensions of Bayesian methods to situations in which biases are of concern. First, a basic misclassification problem

## Practice of Epidemiology

is illustrated using data from a study of sudden infant death syndrome. Bayesian analyses are then given. These analyses can be conducted directly, or by converting actual-data records to

## Performance of Propensity Score Calibration—A Simulation Study

incomplete records and prior distributions to complete-data records, then applying missing-data techniques to the augmented data set. The analyses can easily incorporate any complete ('validation' or second-stage) data that might be available, as well as adjustments for confounding and selection bias. The approach illustrates how conventional analyses depend on implicit certainty that bias

parameters are null and how these implausible assumptions can be

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Glynn<sup>1,2,6</sup>

replaced by plausible priors for bias parameters.

Keywords Bayesian methods, bias, biostatistics, epidemiology, missing data,

American Journal of Epidemiology

Women's Hospital, Harvard Medical School,

<sup>1</sup> Division of Pharmacoepidemiology and Pharmacoeconomics, Brigham and

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Johns Hopkins Bloomberg School of

observational studies, odds ratio, relative risk, risk analysis, risk

Boston, MA.

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assessment, sensitivity analysis, validation

<sup>2</sup> Division of Preventive Medicine, Brigham and Women's Hospital, Harvard Medical School, Boston, MA.

<sup>3</sup> Department of Epidemiology, Harvard School of Public Health, Boston, MA.

semi-Bayes in which explicit priors are used for

<sup>6</sup> Department of Biostatistics, Harvard School of Public Health, Boston, MA.

some, but not all, parameters.<sup>10,30–32</sup> The Gauss

code, libraries and output used for the main analysis

## Practice of Epidemiology Introduction

There is a growing literature on accounting for uncer

<sup>4</sup> Department of Epidemiology, Boston University School of Public Health,

Boston, MA. <sup>5</sup> Research Triangle Institute, Research Triangle Park, NC.

## Adjustment for Missing Confounders in Studies Based on Observational

tainties in epidemiologic studies by using prior distributions (priors) for

parameters that govern bias.<sup>1–26</sup>

below are available at <http://www.ph.ucla.edu/epi/>

Received for publication November 1, 2005; accepted for publication  
July 13, 2006.

## Databases: 2-Stage Calibration Combining Propensity Scores From Primary

Bayesian methods are a natural approach to use of **and Validation Data**

priors, but epidemiologists have gravitated to more informal simulation methods. I here  
provide one approach to Bayesian uncertainty assessment, focusing on data priors in  
order to recast bias analysis as a missing-data problem. This approach shows how bias  
analysis is complementary to validation-study and two-phase (two-stage) analyses, and  
how all

[faculty/greenland/index.htm](http://faculty/greenland/index.htm).

recently introduced propensity score calibration (PSC), which combines propensity scores  
and regression calibration to address

### exposure misclassification

confounding by variables unobserved in the main study by using variables observed in a  
validation study. Here, Conventional analyses

the authors assess the performance of PSC using simulations in settings with and without  
violation of the key Table 1 presents a study of the relation of sudden

assumption of PSC: that the error-prone propensity score estimated in the main study is a  
surrogate for the gold

## A case-control study with

Confounding can be a major source of bias in nonexperimental research. The authors

Hui-Wen Lin\* and Yi-Hau Chen\*

infant death syndrome (SIDS) to maternal antibiotic

\*

standard propensity score (i.e., it contains no additional information on the outcome). The assumption can be

33

Creating  $U$  from  $X$ ,  $Y$  (and  $C$ ):

$$g[P(U|Y, X, C)] \quad 2$$

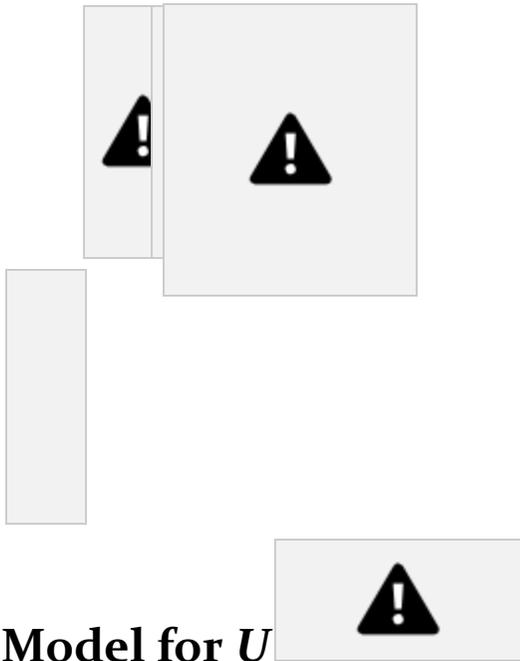
$$= \theta_o + \theta_Y Y + \theta_X X + \theta_{YX} YX + \theta_C C \quad 3$$

for some link function  $g$   $\vdots$   
 $N$

**id U C X Y**  $\vdots$   
 $\cdot$

1

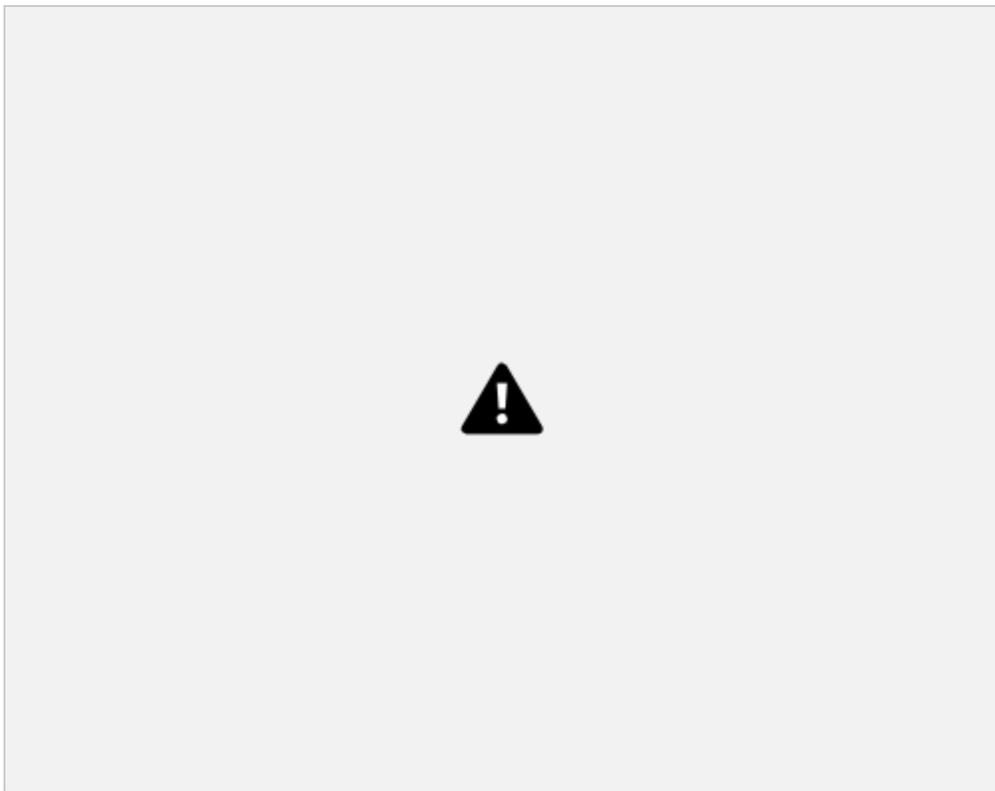
$N$



Model for  $U$

**Missing data methods** recreate  $U$  or some quantity representing adjustment for  $U$  using validation study data or external information

[C]



U



[X]





Many techniques have been developed for study design and analysis to identify and eliminate such errors. Such problems are not expected to compromise experimental

studies, where careful standardization of conditions (for laboratory work) and randomization (for **Negative Controls**

population studies) should, if applied properly, eliminate most such noncausal associations. We argue, however, that a routine precaution taken in the design of biologic laboratory experiments—the use

#### ORIGINAL ARTICLE

of “negative controls”—is designed to detect both suspected and unsuspected sources of spurious causal inference. In epidemiology, analogous negative controls help to identify and resolve confounding as well as other sources of error, including recall bias or analytic flaws. We distinguish 2 types of negative controls (exposure controls

# Negative Controls

and outcome controls), describe examples of each type from the epidemiologic literature, and identify the conditions for the use of conditions that arise in observational studies. Nonexperimental biologists routinely question whether correctly inferred causal relationships from the experiments. Biologists employ “negative controls” as a means of ruling out possible noncausal interpretations. We describe the use of negative controls, highlight some examples of their use in studies, and define the conditions under which negative controls can detect confounding in epidemiologic studies. Although the particular threats to causal inference in experimental and observational science, negative controls is a valuable means of identifying causal associations and can complement other methods for improving causal inference.

## *A Tool for Detecting Confounding and Bias in Observational Studies*

such negative controls to detect confounding. We conclude that negative controls should be more commonly employed in observational studies, and that additional work is needed to specify the

*Marc Lipsitch,<sup>a,b,c</sup> Eric Tchetgen Tchetgen,<sup>a,c,d</sup> and Ted Cohen<sup>a,c,e</sup>*

(*Epidemiology* 2010;21: 383–388)

### **EXPERIMENTAL BIOLOGY: THE CAUSAL INFERENCE AND THE USE OF NEGATIVE CONTROLS**

conditions under which negative controls will be sensitive detectors of other sources of error in observational studies.

**Abstract:** Noncausal associations between exposures and outcomes are a threat to validity of causal inference in observational studies.

In experimental biology, the manipulation of experimental

conditions prevents many of the noncausal associations

that circumvent most threats to the validity of causal

One might imagine that the experimental

*Lipsitch et al Epidemiology • Volume 21, Number 3, May 2010*

Many techniques have been developed for study design and analysis of conditions that arise in observational studies. Nonetheless, exper

**E**pidemiologists seek to distinguish the causal effect of ~~that occur in observational studies~~. For example

to identify and eliminate such errors. Such problems are not expected to compromise experimental studies, where careful standard experimental biologists routinely question whether they have

hypothesis that a particular cytokine—a chemical correctly inferred causal relationships from the results of their

exposure A on outcome Y from associations due to other

signaling in the immune system—enhances the

ization of conditions (for laboratory work) and randomization (for between A and N does not prove unequivocally that the A-Y

population studies) should, if applied properly, eliminate most such association is biased. In the example of using death or

noncausal associations. We argue, however, that a routine precau h d negative control outcome for



recall bias), confounding, and biased selection of individuals tion taken in the design of biologic laboratory experiments—the use of “negative controls”—is designed to detect both suspected and unsuspected sources of spurious causal inference. In epidemiology, analogous negative controls help to identify and resolve confound death or pneumonia/influenza hospitalization,

one could ar ments, highlight some examples of their use in epidemiologic

the cytokine is added, and in condition 2, so

ing as well as other sources of error, including recall bias or analytic compared between conditions 1 and 2.

not think of a plausible one) would create an association in ent in experimental and observational sciences, the use of

experiments. Biologists employ “negative controls” as a species of bacteria by neutrophils, a class o

means of ruling out possible noncausal interpretations of their

categories (in addition to chance)<sup>1</sup>: mismeasurement cells.<sup>2</sup> An experiment is devised in which neu results. We describe the use of negative controls in experi

recall bias), confounding, and biased selection of teria, and growth medium are mixed together. I

gue that there may be some common causes of vaccination studies, and define the conditions under which negative

stance such as saline solution is added. After i and injury that are not causes of all-cause death or pneumo controls can detect confounding in epidemiologic studies.

bacteria are enumerated and the number of

Submitted 19 March 2009; accepted 12 October 2009. can nia/influenza hospitalization. Such common causes (we

Although the particular threats to causal inference are differ

From the <sup>a</sup>Department of Epidemiology, <sup>b</sup>Department of Immunology and

Infectious Diseases, <sup>c</sup>Center for Communicable Disease Dynamics, and flaws. We distinguish 2 types of negative controls (exposure controls

If the investigator finds fewer live bacteri

the negative control analysis of vaccination and injury, even

negative controls is a valuable means of identifying non  
<sup>d</sup>Department of Biostatistics, Harvard School of Public Health, Boston,  
and outcome controls), describe examples of each type from the primary analyses of vaccination and death or pneumo  
1 than in condition 2, the finding is consisif

MA; and <sup>e</sup>Division of Global Health Equity, Brigham and Women's  
epidemiologic literature, and identify the conditions for the use of  
causal associations and can complement other epidemiologic  
Hospital, Boston, MA. unconfounded—thus mak  
hypothesis that the cytokine enhanced  
neutrotonia/influenza hospitalization were

such negative controls to detect confounding. We conclude methods for improving causal inference.  
that

Supported by NIH 5U01GM076497 and 1U54GM088558 (Models of Infec

killing. Nonetheless, concern remains that so

**FIGURE 2.** Causal diagram showing an ideal negative control

negative controls should be more commonly employed in observa  
tious Disease Agent Study) to ML.

neutrophil-mediated killin

outcome N for use in evaluating studies of the causal relation

However, if N is associated only with some, but not all, of the

ing the negative control detect bias even where none exists. than cytokine-aided,

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tional studies, and that additional work is needed to specify the

ship between exposure A and outcome Y. N should ideally

in the HTML and PDF versions of this article ([www.epidem.com](http://www.epidem.com)).

## EXPERIMENTAL BIOLOGY: THREATS TO

sponsible. For example, perhaps there is a cont

conditions under which negative controls will be sensitive detectors  
have the same incoming arrows as Y, except that A does not  
uncontrolled confounders of the association between A and  
of other sources of error in observational studies.

## CAUSAL INFERENCE AND THE USE OF

Y, it is possible that A and N will appear unassociated despite  
cytokine preparation that directly kills bacteri

Correspondence: Marc Lipsitch, Department of Epidemiology, Harvard

cause N; to the extent this criterion is met, N is called

School of Public Health, 677 Huntington Avenue, Boston, MA 02115.

## NEGATIVE CONTROLS

(*Epidemiology* 2010;21: 383–388)  
E-mail: mlipsitc@hsph.harvard.edu.  
U-comparable to Y.

the presence of uncontrolled confounding between A and Y.  
the cytokine itself kills bacteria, or perhaps  
In the influenza vaccine example, one could argue that there  
unintended difference between the treated and

One might imagine that the experimental method would  
pneumonia/  
are common causes of vaccination and death or  
circumvent most threats to the validity of causal inference  
ISSN: 1044-3983/10/2103-0383  
ditions (eg, temperature or pH) caused the di  
that occur in observational studies. For example, consider the  
influenza hospitalization—that are not causes of injury

DOI: 10.1097/EDE.0b013e3181d61eeb

**E**pidemiologists seek to distinguish the causal effect of  
mechanism but is very likely to involve the same sources of



vival of the bacteria.

hypothesis that a particular cytokine—a chemical involved in  
bias that may have been present in the original association. If  
related outcomes. Such a common cause (say, an aversion to  
exposure A on outcome Y from associations due to other  
vaccination that makes an individual less likely to get the  
signaling in the immune system— enhances the killing of a

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Practice of Epidemiology

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◦  
◦

Use of Negative Control Exposure Analysis to Evaluate Confounding: An Example  
of Acetaminophen Exposure and Attention-Deficit/Hyperactivity Disorder in  
Nurses' Health Study II

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Frequent maternal use of acetaminophen in pregnancy has been linked to attention-deficit/hyperactivity disorder (ADHD) in children, but concerns regarding uncontrolled confounding remain. In this article, we illustrate use of the negative control exposure (NCE) approach to evaluate uncontrolled confounding bias in observational studies on pregnancy drug safety and explain the causal assumptions behind the method. We conducted an NCE analysis and evaluated the associations between maternal acetaminophen use during different exposure periods and ADHD among 8,856 children born in 1993–2005 to women enrolled in the Nurses' Health Study II cohort. Information on regular maternal acetaminophen use was collected prospectively in biennial questionnaires. A total of 721 children (8.1%) in the cohort had been diagnosed with ADHD as reported by the mothers. Our NCE analysis suggested that only acetaminophen use at the time of pregnancy was associated with childhood ADHD (odds ratio = 1.34, 95% confidence interval: 1.05, 1.72), and the effect estimates for the 2 NCE periods (about 4 years before and 4 years after the pregnancy) were null. Our findings corroborate those of prior reports suggesting that prenatal acetaminophen exposure may influence neurodevelopment. The lack of an association between acetaminophen

use in the pre- and postpregnancy exposure periods and ADHD provides assurance that uncontrolled time invariant factors do not explain this association.

acetaminophen; attention-deficit/hyperactivity disorder; negative control exposure analysis; neurological development; pregnancy; prenatal exposure delayed effects; uncontrolled confounding



Abbreviations: ADHD, attention-deficit/hyperactivity disorder; NCE, negative control exposure; NHS II, Nurses' Health Study II.

sure and the confounder on the outcome, or having only one unmeasured confounder. Without imposing any assumptions on the unmeasured confounder or confounders, we derive a bounding factor and a sharp inequality such that the sensitivity analysis parameters must satisfy the

## Bounding

inequality if an unmeasured confounder is to explain away the observed effect estimate or reduce it to a particular level. Our approach is easy to

### ORIGINAL ARTICLE

implement and involves only two sensitivity parameters. Surprisingly, our bounding factor, which makes no simplifying assumptions, is no more conservative than a number of previous sensitivity analysis techniques that do make assumptions. Our new bounding factor implies not only the traditional Cornfield conditions that both the relative risk of the

# 4FOTJUJWJUZ "OBMZTJT 8JUIPVU "TTVNQUJPOT

exposure on the confounder and that of the confounder on the outcome must satisfy but also a high threshold that the maximum of these relative risks must satisfy. Furthermore, this new bounding factor can be viewed as a measure of the strength of confounding between the exposure and

*Peng Ding<sup>a</sup> and Tyler J. VanderWeele<sup>b</sup>*

the outcome induced by a confounder.

(*Epidemiology* 2016;27: 368–377)

also often assume a homogeneity assumption that interaction between the effects of the exposure a founder on the outcome.<sup>5–9</sup> Some sensitivity anniques only allow one to assess how strong an confounder would have to be to completely expleffect<sup>1–3,10,11</sup> but do not allow one to assess whaestimate might be under weaker unmeasured cscenarios (i.e., do not allow one to do sensitiviunder alternative hypotheses). Performing sensitivunder alternative hypotheses can be quite challenmore parameters needed in the sensitivity analysisfield et al. early study<sup>1</sup> on sensitivity analysis for tsmoking and lung cancer association, which helthe entire field of sensitivity analysis, in fact masimplifying assumptions: a single binary confinteraction, and only sensitivity analysis for the n

**Abstract:** Unmeasured confounding may undermine the validity of causal inference with observational studies. Sensitivity analysis provides a way to assess the validity of causal inferences even without full control of the confounders of

esis of no causal effect. Although some sensitiv the relationship between the exposure and outcome.

**C**ausal inference with observational studies is of great importance. Although results exist for general confounders,<sup>8,12</sup> they are inter est and importance in many scientific disciplines.

vides an attractive way to partially circumvent this issue by assessing the potential influence of unmeasured confounding on causal conclusions. However, previous sensitivity analysis approaches often make strong Sensitivity analysis plays a central role in assessing the

Although results exist for general confounders,<sup>8,12</sup> they are influence of the unmeasured confounding on the causal con

implement under some of the above simplifying as

In this article, we propose a new bounding clusions. However, many sensitivity analysis techniques often

unmeasured confounding between the exposure and the outcome

sensitivity analysis technique without any a

## Annals of Internal Medicine RESEARCH AND REPORTING METHODS

and untestable assumptions such as having an unmeasured confounder require additional untestable assumptions. For instance, some

may bias the estimation of the true causal effect, an approach about the unmeasured confounder or confounder that is binary, or having no interaction between the effects of the exposure. <sup>1-6</sup> Researchers often called “sensitivity analysis” or “bias analysis” over the assumptions of the null hypothesis, a single unmeasured confounder on the outcome, or having only one also often assume a homogeneity assumption that there is no unmeasured confounder, or no interaction is required for using the of sensitivity parameters sometimes allows researchers to make a bounding factor and a sharp inequality such that confounder. Without imposing any assumptions on the unmeasured confounder. <sup>5-9</sup> Some sensitivity analysis techniques th

## Sensitivity Analysis in Observational Research: Introducing the E-Value

factor. Nonetheless, our new bounding factor, w founder on the outcome. <sup>5-9</sup> Some sensitivity analysis tech Submitted 10 October 2014; accepted 28 January 2016.

no simplifying assumptions, is no more conser  
Tyler J. VanderWeele, PhD, and Peng Ding, PhD  
niques only allow one to assess how strong an unmeasured  
From the <sup>a</sup>Department of Statistics, University of California, Berkeley, CA; many previous sensitivity analysis techniques th  
inequality if an unmeasured confounder is to explain away the observed confounder would have to be to completely explain away an  
and <sup>b</sup>Department of Epidemiology and Biostatistics, Harvard School of

effect estimate or reduce it to a particular level. Our approach is easy to Public Health, assumptions and is furthermore easy to implement  
Boston, MA.  
Sensitivity analysis is useful in assessing how robust an associa effect<sup>1-3,10,11</sup> but do not allow one to assess what the effect  
implement and involves only two sensitivity parameters. The authors propose that in all observational studies intended to  
Surprisingly,

This work was partly supported by National Institutes of Health Grant R01 we show that the new bounding factor implies n  
tion is to potential unmeasured or uncontrolled confounding. our bounding factor, This article introduces a new measure called the “E-value,” which more conservative  
which makes no simplifying assumptions, is no ES017876. than a number of previous sensitivity analysis tech  
produce evidence for causality, the E-value be reported or some

estimate might be under weaker unmeasured confounding other sensitivity analysis be used. They suggest calculating the

scenarios (i.e., do not allow one to do sensitivity analysis

classical Cornfield conditions<sup>1</sup> that both the rela

The authors report no conflicts of interest.

is related to the evidence for causality in observational studies

E-value for both the observed association estimate (after adjust

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the exposure on the confounder and that of the

citations

niques that do make assumptions. Our new factor implies not that are potentially subject to confounding. The E-value is de

bounding

under alternative hypotheses). Performing sensitivity analysis ments for measured confounders) and the limit of the confi

in the HTML and PDF versions of this article ([www.epidem.com](http://www.epidem.com)).

on the outcome must satisfy but also a stronger co

only the traditional Cornfield conditions that both the relative risk of the fined as the minimum strength of association, on the risk ratio

dence interval closest to the null. If this were to become standard

under alternative hypotheses can be quite challenging due to

Correspondence: Peng Ding, Department of Statistics, University of California, exposure on the confounder and that of the confounder on the outcome

the maximum of these relative risks must satisf

more parameters needed in the sensitivity analysis. The Corn

425 Evans Hall, Berkeley, CA 94720. E-mail: [pengdingpku@berkeley.edu](mailto:pengdingpku@berkeley.edu).

scale, that an unmeasured confounder would need to have with must satisfy but also a field et al. early study<sup>1</sup> on sensitivity analysis for the cigarette high threshold that the maximum of these relative both the treatment and the outcome dence from observational studies would improve considerably, to fully explain away a spe Copyright © 2016 Wolters Kluwer Health, Inc. All rights reserved. This is practice, the ability of the scientific community to assess evi risks must satisfy. Furthermore, this new bounding factor can be viewed

confounding between the exposure and the outco

bounding factor can be viewed as a measure of the

cific treatment–outcome association, conditional on the mea smoking and lung cancer association, which helped initiate

and ultimately, science would be strengthened.

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as a measure of the strength of confounding between the exposure and sured covariates. A large E-value implies that considerable un the entire field of sensitivity analysis, in fact made all three

the outcome induced by a confounder.

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from the confounder. We begin by considering ou

measured confounding would be needed to explain away an

where it is permissible to download and share the work provided it is properly

simplifying assumptions: a single binary confounder, no

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effect estimate. A small E-value implies little unmeasured con  
cited. The work cannot be changed in any way or used commercially.

are binary and extend our results further to time-t

(*Epidemiology* 2016;27: 368–377)

interaction, and only sensitivity analysis for the null hypoth

ISSN: 1044-3983/16/2703-0368

non-negative count or continuous outcomes. We co

founding would be needed to explain away an effect estimate.

esis of no causal effect. Although some sensitivity analysis

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ratio and difference scales.

**C**ausal inference with observational studies is of great inter  
est and importance in many scientific disciplines. Although

results exist for general confounders,<sup>8,12</sup> they are only easy to  
implement under some of the above simplifying assumptions.

**M**uch empirical research is concerned with estab  
lishing causation. It is well-known, however, that

unmeasured confounding between the exposure and the outcome may bias the estimation of the true causal effect, an approach with observational data,  
association (1–11) need not im “”

In this article, we propose a new bounding factor and  
feeding may be confounded by smoking behavior or  
sensitivity analysis technique without any assumptions  
by socioeconomic status. In a population-based case– about  
the unmeasured confounder or confounders. None of  
control study, Victora and colleagues (23) examined as



**Bounding methods** aim to provide the limit(s) that the bias due to not

controlling for  $U$  never exceeds, by using a combination of the parameters captured by the **red dashed arrows**

**[C]**



**U**



**[X]**



## Future Directions



- Some challenges that need addressing
  - Making existing and future methods more user-friendly
  - Reasoning about and how to obtain bias parameters and their –

Extension to time-varying confounding settings and g-methods –

Different sources of bias: need for multiple-bias modeling

– How to integrate bias analysis into routine regression procedures –

How to conduct, interpret and report quantitative bias

– How to get journals to accept more nuanced analysis of observational data that incorporates bias analysis

– How to train epidemiologists to see bias analysis as an integral part of any serious causal modeling, not as an after-thought



- Some unfolding and expected future directions
  - Extending Pearl's front door formula: somewhat like using mediating instrumental variable(s) (Pearl 1994, 1995, 2000)
  - Use of a general bias simulation framework: DAG out the data generating process and use it to simulate how much confounding by  $U$  under the causal null (Arah 2017)
  - Data fusion: combining multiple datasets and information within a causal framework (Bareinboim 2016; 2019)
  - New clever designs: e.g. use of multiple synthetic exposure controls with increasingly richer confounder information

- Extending negative control methods to complex exposures and outcomes



DAG: Uncontrolled



Can identify the total effect of  $X$  on  $Y$  provided

(i)  $M$  completely d-separates the

**Front-door criterion:**

confounding of  $X \rightarrow Y$  due to unmeasured  $U$

$M$  d-separates  $X$  and  $Y$

conditional on  $U$

Can be extended to allow for multiple  $M$  and direct arrow from  $X$  to  $Y$ : total unidentified but the effect of  $X$  on  $Y$  through  $M$  would be

causal path(s) from  $X$  to  $Y$

(ii) no uncontrolled confounding of confounders



$X \square M$

(ii) no uncontrolled confounding of  $M \square Y$  given  $X$

(Pearl 1994, 1995, 2009)

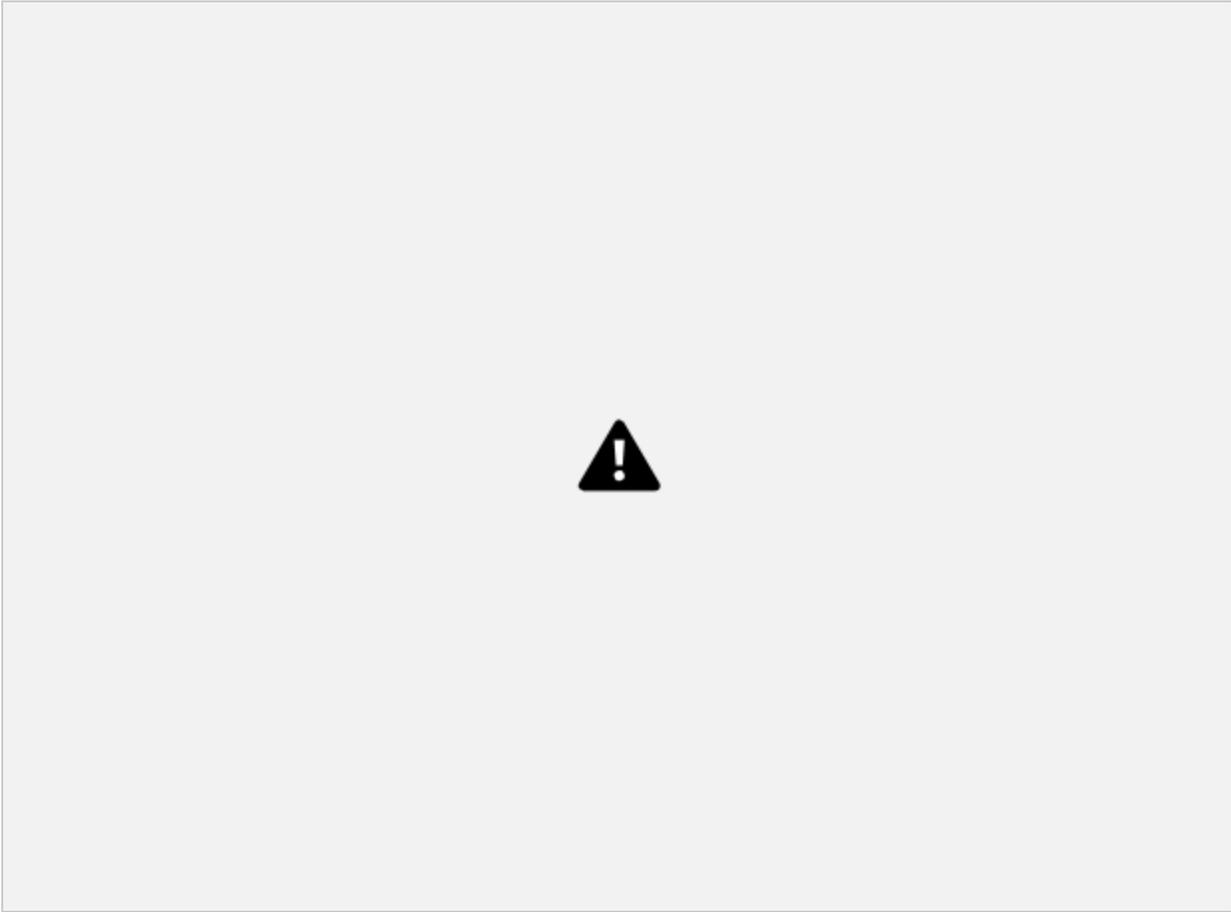
**Modified (i):**  $M$  d-separates a specific causal path from  $X$  to  $Y$

**Modified (i) and (ii):** Both conditional on measured

**C U**



**X**



**Y**



*Annu Rev Public Health 2017*



# Conclusion



- Bias analysis is becoming more important given the rise of big data, cheap computing and automated algorithms (including AI), new bias methods, and causal inference
- Given the increased use of very large datasets in epidemiology, we need methods for **reducing the chances of being precisely wrong**: we need **sophisticated and transparent quantitative bias analysis**

- **Bias analysis is a stress test for credible causal inference:** *What else could explain our results from observational studies?*



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